

IX
DAR CENTENARY PUBLIC SCHOOL
UMA (98)

- Q1 Factorise : $4\sqrt{3}x^2 + 5x - 2\sqrt{3}$.
- Q2. If $4x^3 + 7x^2 - 3x - 6$ is divided by $x+1$, then find the quotient.
- Q3. If $a-b=7$ and $a^2+b^2=85$, find a^3-b^3 .
- Q4 Factorise: $(p+q)^2 - 20(p+q) - 125$.
- Q5. The volume of a cuboid is polynomial $p(x) = 8x^3 + 12x^2 - 2x - 3$. Find the possible expression for the dimension of the cuboid. Verify the result by taking $x=5$ units.
- Q6. If p and q be the remainders, when the polynomials $x^3 + 2x^2 - 5ax - 7$ and $x^3 + ax^2 - 12x + 6$ are divided by $(x+1)$ and $(x-2)$ respectively. If $2p+q=6$, find the value of a .
- Q7 If a, b and c are all non-zero but their sum is zero, then show that $\frac{a^2}{bc} + \frac{b^2}{ca} + \frac{c^2}{ab} = 3$.
- Q8 Using Heron's formula, find the area of an equilateral \triangle with side 16 cm.
- Q9. Find area of triangle whose sides are 13 cm, 14 cm, 15 cm.
- Q10 Three vertices of a rectangle are $(3, 2)$, $(-4, 2)$ and $(-4, 5)$. Plot these points and find the co-ordinates of fourth vertex.
- Q11 The sides of a triangular plate are 8 cm, 15 cm and 17 cm. If its weight is 96 gm. Find the weight of plate per sq. cm.
- Q12 If the polynomial $f(x) = px^3 + 4x^2 + 3x - 4$ and $g(x) = x^3 - 4x + p$ are divided by $(x-3)$, then remainder in each case is same. Find the value of p .
- Q13. Let R_1 and R_2 are remainders when polynomial $f(x) = 4x^3 + 3x^2 - 12ax - 5$ and $g(x) = 2x^3 + ax^2 - 6x + 2$ are divided by $(x-1)$ and $(x+2)$ respectively. If $3R_1 + R_2 + 28 = 0$, find the value of ' a '.
- Q14 Find the value of k , if $(x-3)$ is a factor of $k^2x^2 - kx - 2$.
- Q15 Factorise: i) $y^3 - 7y + 6$. ii) $x^3 + 13x^2 + 32x + 20$
- Q16 If $(x-2)$ and $(x-\frac{1}{2})$ are factors of $px^2 + 5x + 2$, show that $p=2$.
- Q17 Expand: $(-2x+3y+2z)^2$
- Q18 Verify that: $x^3+y^3+z^3-3xyz = \frac{1}{2}(x+y+z)[(x-y)^2 + (y-z)^2 + (z-x)^2]$
- Q19 Resolution factors: $1+a+b+c+ab+bc+ca+abc$.

Q20 factors of $x^6 - y^6$:

Q21 Three vertices of square are P(-1, -9), Q(3, -1), R(-5, 3). Plot the points. Also find the co-ordinate of missing vertex D.

Q22 Name the quadrant / axis in which the points lies:

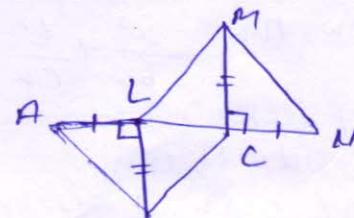
$$(1, 1); (0, 5); (-2, -4); (1, -2); (-2, 0)$$

Q23. Write the x-co-ordinate of a point lie on y-axis.

Q24. Plot the points A(2, 0), B(2, 2), C(0, 2) and draw the line segments OA, AB, BC and CO. What do you obtain? Find its Area.

Q25. Find the co-ordinates of vertices of ~~rectangle~~ rectangle placed in III quadrant in cartesian plane with length 'p' unit of x-axis and breadth 'q' unit on y-axis.

Q26 In the figure $BL \perp AC$, $MC \perp LN$, $AL = CN$ and $BL = CM$. Prove that $\triangle ABC \cong \triangle NML$



Q27. Prove that angles opposite to equal sides of an isosceles triangle are equal.

Q28. In $\triangle ABC$ is an isosceles \triangle with $AB = AC$, side BA is produced to D such that $AB = AD$. Prove that $\angle BCD$ is a right-angle.

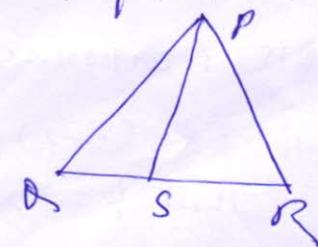
Q29. Prove that two triangle are congruent if any two angles and included side of one triangle is equal to any two angles and included side of the other triangle.

Q30 AB and CD are respectively the smallest and longest side of quadrilateral ABCD (see fig.)

Show that $\angle A > \angle C$ and $\angle B > \angle D$.

Q31 Show that in a right-angled \triangle hypotenuse is the longest side.

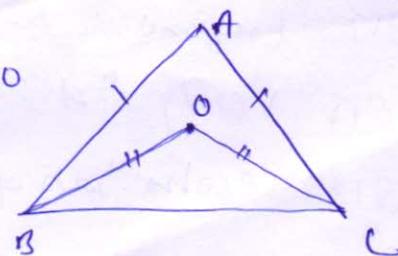
Q32. In the figure 'S' is any point on the side QR of $\triangle PQR$. Prove that $PQ + QR + RP > 2PS$



Q33 In $\triangle ABC$, D is mid point of side AC such that $BD = \frac{1}{2}AC$

Show that $\angle ABC$ is right angle.

Q34 In the given figure, find ratio $\angle ABO : \angle ACO$



VNA (H.P)

Q1. Simplify: $\left(\frac{81}{16}\right)^{-\frac{3}{4}} \times \left(\frac{25}{9}\right)^{-\frac{3}{2}}$

Q2. Find the square root of 4.7 geometrically.

Q3. If $\sqrt{5} = 2.235$ and $\sqrt{10} = 3.162$, find the value of

$$\left(\frac{\sqrt{10} - \sqrt{5}}{\sqrt{2}} \right)$$

Q4. Find a rational number between $-\frac{3}{7}$ and $\frac{1}{3}$.

Q5. Simplify: $\left[\left\{ \left(625 \right)^{-\frac{1}{2}} \right\}^{-\frac{1}{4}} \right]^2$

Q6. Simplify: $\left\{ (-2)^0 + (5)^0 + (-13)^0 \right\}^{-2}$

Q7. If $x^{\frac{1}{12}} = 49^{\frac{1}{24}}$, find the value of x .

Q8. Represent $1 + \sqrt{3}$ on the number line.

Q9. Simplify: $\sqrt[4]{81} - 8\sqrt[3]{216} + 15\sqrt[5]{32} + \sqrt{225}$

Q10. Locate $\sqrt{17}$ on the number line.

Q11. Express 15.725 in the form $\frac{p}{q}$ where p and q are integers.

Q12. Express $1.\overline{32} + 0.\overline{35}$ as a fraction in simplest form.

Q13. Find 'n', if $2^{n-7} \times 5^{n-4} = 1250$.

Q14. Simplify: $\frac{1}{\sqrt{5} + \sqrt{6} - \sqrt{11}}$ [Ans. $\frac{\sqrt{5} + 6\sqrt{5} + \sqrt{330}}{60}$]

Q15. Simplify: $\frac{1}{2+\sqrt{5}} + \frac{1}{\sqrt{5}+\sqrt{6}} + \frac{1}{\sqrt{6}+\sqrt{7}} + \frac{1}{\sqrt{7}+\sqrt{8}}$ [Ans. $(-2+\sqrt{8})$]

Q16. Find the value of a and b , if $\frac{7+3\sqrt{5}}{3+\sqrt{5}} + \frac{7-3\sqrt{5}}{3-\sqrt{5}} = a + b\sqrt{5}$.

Q17. If $x = \frac{\sqrt{p+q} + \sqrt{p-q}}{\sqrt{p+q} - \sqrt{p-q}}$, then prove that [Ans. $a=3$, $b=0$]

$$qx^2 - 2px + q = 0$$

Q18. If $a = 7 - 4\sqrt{3}$, find the value of $\sqrt{a} + \frac{1}{\sqrt{a}}$.

Q19. Simplify: $\frac{2^{x+1} + 2^x}{2^{x+1} - 2^x}$

Q20. Prove that $\frac{1}{1+n^{c-a} + n^{b-c}} + \frac{1}{1+n^{a-b} + n^{c-b}} + \frac{1}{1+n^{a-c} + n^{b-c}} = 1$

Q21. Show that $(n^{p+q})^{p-q} \times (n^{q+r})^{q-r} \times (n^{r+p})^{r-p} = 1$

Q22. Define the following terms: (i) Parallel lines (ii) intersecting lines.
 (iii) line segment (iv) square. (v) radius.

Q23. Prove that two distinct lines cannot have more than one point in common.

Q24. Write all the five postulates of Euclid.

Q25. Does Euclid's fifth postulate imply the existence of parallel lines. Explain.

Q26. Show that every line segment has one and only one mid point.

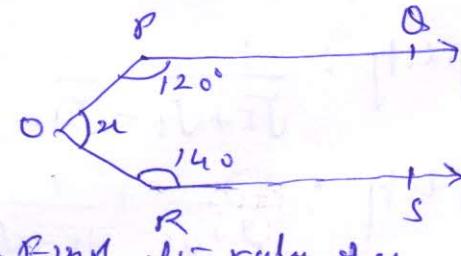
Q27. Prove that vertically opposite angles are equal.

Q28. Prove that sum of 3 angles of a \triangle is 180° .

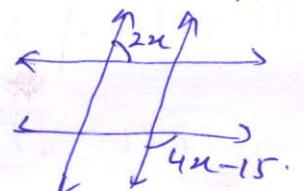
Q29. Prove that sum of three exterior angle of a \triangle is 360° .

Q30. Two parallel lines are intersected by a transversal.
 Prove that the bisectors of two pairs of interior angles enclose a rectangle.

Q31. In the figure $PQ \parallel RS$, find x



Q32. In the fig. $\angle 1 \cong \angle 2$ and $a \cong d$. Find the value of x



Q33. In the given figure, $AB \parallel CD$ and $CD \parallel EF$. Also $EA \perp AB$. If $\angle BEF = 55^\circ$
 find the value of x, y and z

