CLASS X (2020-21) **MATHEMATICS STANDARD (041)** SAMPLE PAPER-07

Time: 3 Hours

General Instructions :

- 1. This question paper contains two parts A and B.
- 2. Both Part A and Part B have internal choices.

Part-A:

- 1. It consists of two sections- I and II.
- 2. Section I has 16 questions. Internal choice is provided in 5 questions.
- Section II has four case study-based questions. Each case study has 5 case-based sub-parts. An examinee is to 3. attempt any 4 out of 5 sub-parts.

Part-B:

1. Question no. 21 to 26 are very short answer type questions of 2 mark each.

[Board Term-1 2016]

- Question no. 27 to 33 are short answer type questions of 3 marks each. 2.
- Question no. 34 to 36 are long answer type questions of 5 marks each. 3.
- 4. Internal choice is provided in 2 questions of 2 marks, 2 questions of 3 marks and 1 question of 5 marks.

Part - A

Section - I

What is the condition for the decimal expansion of a 1. rational number to terminate? Explain with the help of an example.

The decimal expansion of a rational number terminates, if the denominator of rational number can be expressed as $2^m 5^n$ where m and n are non negative integers and p and qboth co-primes.

e.g.

$$\frac{3}{10} = \frac{3}{2^1 \times 5^1} = 0.3$$

Find a quadratic polynomial, whose zeroes are -32. and 4?

Ans :

We have $\alpha = -3$ and $\beta = 4$.



 $\alpha + \beta = -3 + 4 = 1$ Sum of zeros $\alpha \cdot \beta = -3 \times 4 = -12$ Product of zeros,

So, the quadratic polynomial is

$$x^{2} - (\alpha + \beta)x + \alpha\beta = x^{2} - 1 \times x + (-12)$$
$$= x^{2} - x - 12$$
$$= \frac{x^{2}}{2} - \frac{x}{2} - 6$$

3. In given figure, the graph of a polynomial p(x) is shown. Calculate the number of zeroes of p(x).



[Board Term-1 2013] Ans : The graph intersects x-axis at one point x = 1. Thus the number of zeroes of p(x) is 1.

Find the roots of the quadratic 4. equation $\sqrt{3} x^2 - 2x - \sqrt{3} = 0$

) = 0

We have

Ans :

$$\sqrt{3} x^2 - 2x - \sqrt{3} = 0$$

$$\sqrt{3} x^2 - 3x + x - \sqrt{3} = 0$$

$$\sqrt{3} x(x - \sqrt{3}) + 1(x - \sqrt{3}) = 0$$

$$(x - \sqrt{3})(\sqrt{3} x + 1) = 0$$

$$x = \sqrt{3}, \frac{-1}{\sqrt{3}}$$



Thus

Find the value of k, for which one root of the quadratic equation $kx^2 - 14x + 8 = 0$ is six times the other. [Board Term-2, 2016] Ans :

We have $kx^2 - 14x + 8 = 0$

Maximum Marks: 80

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Let one root be α and other root be 6α .

Sum of roots,

$$7\alpha = \frac{14}{k}$$
 or $\alpha = \frac{2}{k}$...(1)

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Product of roots, $\alpha(6\alpha) = \frac{8}{k}$ or $6\alpha^2 = \frac{8}{k}$

 $\alpha + 6\alpha = \frac{14}{1}$

Solving (1) and (2), we obtain

$$6\left(\frac{2}{k}\right)^2 = \frac{8}{k}$$

$$6 \times \frac{4}{k^2} = \frac{8}{k}$$

$$\frac{3}{k^2} = \frac{1}{k}$$

$$3k = k^2$$

$$3k - k^2 = 0$$

$$k[3 - k] = 0$$

$$k = 0 \text{ or } k = 3$$

Since k = 0 is not possible, therefore k = 3.

5. Is series $\sqrt{3}, \sqrt{6}, \sqrt{9}, \sqrt{12}, \dots$ an AP? Give reason. Ans : [Board Term-2 2015]

Let common difference be *d* then we have $d = a_2 - a_1 = \sqrt{6} - \sqrt{3} = \sqrt{3}(\sqrt{2} - 1)$ $d = a_3 - a_2 = \sqrt{9} - \sqrt{6} = 3 - \sqrt{6}$ $d = a_4 - a_3 = \sqrt{12} - \sqrt{9} = 2\sqrt{3} - 3$

As common difference are not equal, the given series is not in AP.

 \mathbf{or}

What is the next term of an AP $\sqrt{7}$, $\sqrt{28}$, $\sqrt{63}$,....? Ans: [Board Term-2 Foreign 2014]

Let the first term of an AP be a and common difference be d.

Here,

$$a = \sqrt{7}, a + d = \sqrt{28}$$

$$d = \sqrt{28} - \sqrt{7} = 2\sqrt{7} - \sqrt{7}$$

$$= \sqrt{7}$$
Next term
$$= \sqrt{63} + \sqrt{7}$$

$$= 3\sqrt{7} + \sqrt{7} = 4\sqrt{7}$$

$$= \sqrt{7 \times 16}$$

$$= \sqrt{112}$$

6. In Figure, $DE \mid \mid BC$. Find the length of side AD, given that AE = 1.8 cm, BD = 7.2 cm and CE = 5.4 cm.



Sample Paper 07 Solved

Since $DE \mid \mid BC$ we have

$$\frac{AD}{DB} = \frac{AE}{EC}$$

Substituting the values, we get

$$\frac{AD}{7.2} = \frac{1.8}{5.4}$$
$$AD = \frac{1.8 \times 7.2}{5.4} = \frac{12.96}{5.4} = 2.4 \text{ cm}$$

7. If the mid-point of the line segment joining the points A(3, 4) and B(k, 6) is P(x, y) and x + y - 10 = 0, find the value of k.

If P(x, y) is mid point of A(3, 4) and B(k, 6), then we have

$$\frac{3+k}{2} = x$$
 and $y = \frac{4+6}{2} = \frac{10}{2} = 5$

Substituting above value in x + y - 10 = 0 we have

$$\frac{3+k}{2} + 5 - 10 = 0$$

$$\frac{3+k}{2} = 5$$

$$3+k = 10 \Rightarrow k = 10 - 3 = 7$$

8. The ordinate of a point A on y-axis is 5 and B has co-ordinates (-3,1). Find the length of AB.

[Board Term-2 2014]

We have A(0,5) and B(-3,1).

Ans :

Ans :

Distance between A and B,

AB

and B,

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(-3 - 0)^2 + (1 - 5)^2}$$

$$= \sqrt{9 + 16}$$

$$= \sqrt{25} = 5$$

9. If $\sec \theta \cdot \sin \theta = 0$, then find the value of θ .

[Board Term-1 2016]

We have $\sec \theta \cdot \sin \theta = 0$

$$\frac{1}{\cos\theta} \cdot \sin\theta = 0$$
$$\frac{\sin\theta}{\cos\theta} = 0$$

$$\tan \theta = 0 = \tan \theta$$

Thus $\theta = 0^{\circ}$

Ans :

Ans :

We have

10. If A and B are acute angles and $\sin A = \cos B$, then find the value of A + B.

.0°

We have $\begin{aligned}
\sin A &= \cos B \\
\sin A &= \sin(90^\circ - B) \\
A &= 90^\circ - B \\
A + B &= 90^\circ
\end{aligned}$

11. If $\tan(A+B) = \sqrt{3}$ and $\tan(A-B) = \frac{1}{\sqrt{3}}$, A > B, then the value of A is

[Board 2020 Delh] $\tan(A+B) = \sqrt{3}$

...(1)

$$= \tan 60^{\circ}$$

 $= \tan 30^{\circ}$

Α

$$\tan\left(A - B\right) = \frac{1}{\sqrt{3}}$$

 $A+B = 60^{\circ}$

$$A - B = 30^{\circ} \qquad \dots (2)$$

Adding equation (1) and (2) we get
$$2A = 90^{\circ} \Rightarrow A = 45^{\circ}$$

12. Two tangents making an angle of 60° between them are drawn to a circle of radius $\sqrt{3}$ cm, then find the length of each tangent.

Ans: [Board, Term-2, 2013]

As per the given question we draw the figure as below.



Since,

t

So.

$$\tan \theta = \frac{OA}{AP}$$

$$\tan 30^{\circ} = \frac{OA}{AP}$$

$$\frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{AP}$$

$$AP = \sqrt{3} \times \sqrt{3} = 3 \text{ cm.}$$

or

In figure, AP and BP are tangents to a circle with centre O, such that AP = 5 cm and $\angle APB = 60^{\circ}$. Find the length of chord AB.

Ans :

[Board Term-2 Delhi 2016]

B

Since length of 2 tangents drawn from an external point to a circle are equal, we have

PB

0

$$PA =$$

Thus
$$\angle PAB = \angle PBA = 60^{\circ}$$

Hence $\triangle PAB$ is an equilateral triangle
Therefore $AB = PA = 5$ cm.



13. Two coins of diameter 2 cm and 4 cm respectively are kept one over the other as shown in the figure, find the area of the shaded ring shaped region in square cm.



Ans :

Ans :

Ans :

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Area of circle $= \pi r^2$ Area of the shaded region $= \pi (2)^2 - \pi (1)^2$ $=4\pi - \pi = 3\pi$ sq cm

or

The diameter of two circle with centre A and B are 16 cm and 30 cm respectively. If area of another circle with centre C is equal to the sum of areas of these two circles, then find the circumference of the circle with centre C.

[Board Term-2 2012]

Let the radius of circle with centre C be r. According to question we have

$$\pi(8)^2 + \pi(15)^2 = \pi r^2$$

$$64\pi + 225\pi = \pi r^2$$

$$289\pi = \pi r^2$$

$$R^2 = 289$$
 or $R = 17$ cm

Circumference of circle

$$2\pi r = 2\pi \times 17$$
$$= 34\pi \text{ cm}$$

14. The radii of two cylinders are in the ratio 2 : 3 and their heights are in the ratio 5 : 3, find the ratio of their volumes.

[Board Term-2 2012]

$$\frac{\text{Volume of } 1^{\text{st}} \text{cylinder}}{\text{Volume of } 2^{\text{nd}} \text{cylinder}} = \frac{\pi n_1^2 h_1}{\pi n_2^2 h_2}$$
$$= \left(\frac{n_1}{n_2}\right)^2 \times \frac{h_1}{h_2}$$
$$= \left(\frac{2}{3}\right)^2 \times \frac{5}{3}$$
$$= \frac{4}{9} \times \frac{5}{3} = \frac{20}{27}$$

= 20 : 27

15. Find the mean of the data using an empirical formula when it is given that mode is 50.5 and median in 45.5. Ans : [Board Term-1 2015]

Mode,	M = 50.5	
Median,	$M_d~=45.5$	
Now	$3M_d=M_o+2M$	
	$3 \times 45.5 = 50.5 + 2M$	n160
Mean,	$M = \frac{136.5 - 50.5}{2} = 43$	



Hence mean is 43.

16. Cards marked with number 3, 4, 5,, 50 are placed in a box and mixed thoroughly. A card is drawn at random from the box. Find the probability that the selected card bears a perfect square number.
Ans : [Board Term-2 2016]

Total number of outcomes,

n(S) = 48

Favourable outcomes are 4, 9, 16, 25, 36 and 49. No. of favourable outcomes,

$$n(E) = 6$$

P(perfect square number),

$$P(E) = \frac{n(E)}{n(S)} = \frac{6}{48} \text{ or } = \frac{1}{8}$$

or

20 tickets, on which numbers 1 to 20 are written, are mixed thoroughly and then a ticket is drawn at random out of them. Find the probability that the number on the drawn ticket is a multiple of 3 or 7.

Ans :

Total number of cases,

$$n(S) = 20$$



Favourable outcome,

$$E = \{3, 6, 7, 9, 12, 14, 15, 18\}$$

[Board Term-2 Foreign 2016]

Number of favourable cases,

n(E) = 8Required probability,

$$P(E) = \frac{n(E)}{n(S)} = \frac{8}{20} = \frac{2}{5}$$

Section II

Case study-based questions are compulsory. Attempt any 4 sub parts from each question. Each question carries 1 mark.

17. The Republic Day parade, first held in 1950, has been a yearly ritual since. The parade marches from the Rashtrapati Bhawan along the Rajpath in New Delhi. Several regiments of the army, navy, and air force, along with their bands, march to India Gate. The parade is presided over by the President of India, who is the Commander-in-Chief of the Indian Armed Forces. As he unfurls the tricolour, the national anthem is played. The regiments of the Armed Forces then start their march past. Prestigious awards like Kirti Chakra, Ashok Chakra, Paramvir Chakra and Vir Chakra are given out by the President. Nine to twelve different regiments of the Indian Army, in addition to the Navy and Air Force march toward India Gate along with their bands. Contingents of paramilitary forces and other civil forces also participate in the parade.



On 71th republic day parade, captain RS Meel is planing for parade of following two group:

- (a) First group of Army troops of 624 members behind an army band of 32 members.
- (b) Second group of CRPF troops with 468 soldiers behind the 228 members of bikers.

These two groups are to march in the same number of columns. This sequence of soldiers is followed by different states Jhanki which are showing the culture of the respective states.

(i) What is the maximum number of columns in which the army troop can march?

(a) 8 (b) 16



(ii) What is the maximum number of columns in which the CRPF troop can march?

(d) 32

(a) 4 (b) 8 (c) 12 (d) 16

(c) 4

- (iii) What is the maximum number of columns in which total army troop and CRPF troop together can march past?
 - (a) 2 (b) 4
 - (c) 6 (d) 8
- (iv) What should be subtracted with the numbers of CRPF soldiers and the number of bikers so that their maximum number of column is equal to the maximum number of column of army troop?
 - (a) 4 Soldiers and 4 Bikers
 - (b) 4 Soldiers and 2 Bikers
 - (c) 2 Soldiers and 4 Bikers
 - (d) 2 Soldiers and 2 Bikers
- (v) What should be added with the numbers of CRPF soldiers and the number of bikers so that their maximum number of column is equal to the maximum number of column of army troop?(a) 4 Soldiers and 4 Bikers
 - (b) 12 Soldiers and 12 Bikers
 - (c) 6 Soldiers and 6 Bikers
 - (d) 12 Soldiers and 6 Bikers

Ans :

(i) We will find the HCF (624, 32) = 16

Thus (b) is correct option.

(ii) We will find the HCF (228, 468) = 12.

Thus (c) is correct option. According to the question, we have to find out

HCF(624, 32, 228, 468) = 4

(iii) Alternatively we can find,

HCF (16, 12) = 4

Thus (b) is correct option.

(iv) Maximum number of column of army troop is 16. But 228 and 468 are not divisible by 16. If we subtract 4 from 228 and 468, both(224 and 464) are divisible by 16.

Thus (a) is correct option.

(v) Maximum number of column of army troop is 16. But 228 and 468 are not divisible by 16. If we add 12 in 228 and 468, both(240 and 480) are divisible by 16. Thus (b) is correct option.

18. Dipesh bought 3 notebooks and 2 pens for Rs. 80. His friend Ramesh said that price of each notebook could be Rs. 25. Then three notebooks would cost Rs.75, the two pens would cost Rs. 5 and each pen could be for Rs. 2.50. Another friend Amar felt that Rs. 2.50 for one pen was too little. It should be at least Rs. 16. Then the price of each notebook would also be Rs.16.



Aditya also bought the same types of notebooks and pens as Dipesh. He paid 110 for 4 notebooks and 3 pens.

- (i) Whether the estimation of Ramesh and Amar is applicable for Aditya?
 - (a) Ramesh's estimation is wrong but Amar's estimation is correct.
 - (b) Ramesh's estimation is correct but Amar's estimation is wrong.
 - (c) Both estimation are correct.
 - (b) Ramesh's estimation is wrong but Amar's estimation is also wrong.
- (ii) Let the cost of one notebook be x and that of pen be y. Which of the following set describe the given problem ?
 - (a) 2x + 3y = 80 and 3x + 4y = 110
 - (b) 3x + 2y = 80 and 4x + 3y = 110
 - (c) 2x + 3y = 80 and 4x + 3y = 110
 - (d) 3x + 2y = 80 and 3x + 4y = 110
- (iii) What is the exact cost of the notebook?
 - (a) Rs 10
 - (b) Rs 20
 - (c) Rs 16 $\,$
 - (d) Rs 24

0¢X

- (iv) What is the exact cost of the pen?
 - (a) Rs 10 (b) Rs 20 (c) Rs 16 (d) Rs 24

- (v) What is the total cost if they purchase the same type of 15 notebooks and 12 pens.
 (a) Rs 410
 (b) Rs 200
 - (c) Rs 420 (d) Rs 240

Ans :

(i) Consider the prices mentioned by Ramesh. If the price of one notebook is Rs. 25 and the price of one pen is Rs. 2.50 then,

The cost of 4 notebooks would be : $4\times 25=100~\mathrm{Rs}$

- And the cost for 3 pens would be : $3 \times 2.5 = 7.5$ Rs
- Aditya should have paid 100 + 7.5 = 107.5 Rs.

But he paid Rs. 110, thus Ramesh's estimation is wrong.

- Now, consider the prices mentioned by Amar.
- The cost of 4 notebooks, if one is for Rs.16, would be : $4 \times 16 = 64$ Rs

And the cost for 3 pens, if one is for Rs. 16, would be : $3 \times 16 = 64$ Rs

Aditya should have paid 64 + 48 = 112 Rs but this is more than the price he paid.

Therefore, Amar's estimation is also wrong.

Thus (d) is correct option.

(ii) According to the statement, we have

3x + 2y = 80 and 4x + 3y = 110

Thus (b) is correct option.

(iii) Solving 3x + 2y = 80 and 4x + 3y = 110 we get x = 20 and y = 10

Thus cost of 1 notebook is 20 Rs and cost of 1 pen is 10 Rs

- Thus (b) is correct option.
- (iv) Cost of 1 pen = Rs. 10
- Thus (a) is correct option.
- (v) Total cost $15 \times 20 + 12 \times 10 = 420$ Rs

Thus (c) is correct option.

19. Ajay, Bhigu and Colin are fast friend since childhood. They always want to sit in a row in the classroom . But teacher doesn't allow them and rotate the seats row-wise everyday. Bhigu is very good in maths and he does distance calculation everyday. He consider the centre of class as origin and marks their position on a paper in a co-ordinate system. One day Bhigu make the following diagram of their seating position.



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- (i) What are the coordinates of point A? (a) (2,2)
 - (b) (2, -2)
 - (c) (-2,2)
 - (d) (-2, -2)

- (ii) What is the distance of point A from origin ? (b) $2\sqrt{2}$ (a) 8 (d) $4\sqrt{2}$ (c) 4
- (iii) What is the distance between A and B? (a) $3\sqrt{19}$ (b) $3\sqrt{5}$

(c) $\sqrt{17}$ (d)	2
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- (iv) What is the distance between B and C? (a) $3\sqrt{19}$ (b) $3\sqrt{5}$ (c) $2\sqrt{17}$ (d) $2\sqrt{5}$
- (v) A point D lies on the line segment between points A and B such that AD: DB = 4:3. What are the the coordinates of point D?

(a)
$$\left(\frac{10}{7}, \frac{2}{7}\right)$$
 (b) $\left(\frac{2}{7}, \frac{7}{7}\right)$
(c) $\left(-\frac{10}{7}, -\frac{2}{7}\right)$ (d) $\left(-\frac{2}{7}, -\frac{7}{7}\right)$

Ans :

(i) It may be seen easily from figure that coordinates of point A are (-2,2).

Thus (c) is correct option.

(ii)
$$OA = \sqrt{(0+2)^2 + (0-2)^2} = 2\sqrt{2}$$

Thus (b) is correct option.

(iii) It may be seen easily from figure that coordinates of point A are (-1, -2).

$$AB = \sqrt{(-2+1)^2 + (2+2)^2}$$
$$= \sqrt{1+4^2} = \sqrt{17}$$

Thus (c) is correct option. (iv) It may be seen easily from figure that coordinates of point A are (0, 3).

$$BC = \sqrt{(-1-3)^2 + (-2-0)^2}$$
$$= \sqrt{4^2 + 4} = 2\sqrt{5}$$

Thus (d) is correct option.

(v) We have A(-2,2) and B(-1,-2)

$$\frac{m}{n} = \frac{4}{3}$$

$$x = \frac{mx_2 + nx_1}{m + n} = \frac{-1(4) + 3(-2)}{4 + 3} = \frac{-10}{7}$$

$$y = \frac{my_2 + hy_1}{m + n} = \frac{-2(4) + 3(2)}{4 + 3} = \frac{-2}{7}$$

Thus (c) is correct option.

20. Radio towers are used for transmitting a range of communication services including radio and television. The tower will either act as an antenna itself or support one or more antennas on its structure, including microwave dishes. They are among the tallest humanmade structures. There are 2 main types: guyed and self-supporting structures.

On a similar concept, a radio station tower was built in two sections A and B. Tower is supported by wires from a point O. Distance between the base of the tower and point O is 36 m. From point O, the angle of elevation of the top of section B is 30° and the angle of elevation of the top of section A is 45° .



- (i) What is the height of the section B? (a) $12\sqrt{3}$ m (b) $12\sqrt{2}$ m (c) $8\sqrt{3}$ m (d) $4\sqrt{2}$ m
- (ii) What is the height of the section A? (a) $12(2-\sqrt{2})$ (b) $24(2-\sqrt{2})$ (d) $24(3-\sqrt{3})$ (c) $12(3-\sqrt{3})$
- (iii) What is the length of the wire structure from the point O to the top of section A?
 - (a) $32\sqrt{2}$ m (b) $24\sqrt{3}$ m (c) $28\sqrt{3}$ m (d) $36\sqrt{2}$ m

(iv) What is the length of the wire structure from the point O to the top of section B?

(a) $12\sqrt{3}$ m	(b) $24\sqrt{3}$ m
(c) $28\sqrt{3}$ m	(d) $16\sqrt{3}$ m

- (v) What is the angle of depression from top of tower to point O?
 - (a) 30° (b) 45°
 - (c) 15° (d) 75°

Ans :

(i) We make the following diagram as per given information.



In
$$\triangle BCO$$
 $\tan 30^{\circ} = \frac{BC}{OC}$
 $BC = OC \tan 30^{\circ}$
 $BC = 36 \times \frac{1}{\sqrt{3}} = 12\sqrt{3}$ m
Thus (a) is correct option.

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...(1)(2)

(ii) In
$$\Delta ACO$$
,

$$\tan 45^\circ = \frac{AC}{OC} = 1$$

 $AC = OC = 36 \,\mathrm{m}$

Thus

AB = AC - BCNow,

$$= 36 - 12\sqrt{3} = 12(3 - \sqrt{3})$$
 m
Thus (c) is correct option.

(iii) In ΔACO ,

$$\cos 45^{\circ} = \frac{OC}{OA}$$
$$\frac{1}{\sqrt{2}} = \frac{36}{OA}$$

$$OA = 36\sqrt{2}$$
 m

Thus (d) is correct option.

(iv) In ΔBCO ,

$$\cos 30^{\circ} = \frac{OC}{OB}$$
$$\frac{\sqrt{3}}{2} = \frac{36}{OB}$$
$$OB = \frac{72}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 24\sqrt{3} \text{ m}$$

Thus (b) is correct option.

(v) It is clear from figure that angle of elevation from point O to top of tower is 45° . This is equal to the angle of depression from top of tower to point O. Thus (b) is correct option.

Part - B

All questions are compulsory. In case of internal choices, attempt anyone.

21. If m and n are the zeroes of the polynomial $3x^2 + 11x - 4$, find the value of $\frac{m}{n} + \frac{n}{m}$. Board Term-1 2012 Ans :

We have
$$\frac{m}{n} + \frac{n}{m} = \frac{m^2 + n^2}{mn} = \frac{(m+n)^2 - 2mn}{mn} (1)$$

Sum of zeroes $m+n = -\frac{11}{3}$

 $mn = \frac{-4}{2}$

Product of zeroes

Substituting in (1) we have

$$\frac{m}{n} + \frac{n}{m} = \frac{(m+n)^2 - 2mn}{mn}$$
$$= \frac{(-\frac{11}{3})^2 - \frac{-4}{3} \times 2}{\frac{-4}{3}}$$
$$= \frac{121 + 4 \times 3 \times 2}{-4 \times 3}$$
$$\frac{m}{n} + \frac{n}{m} = \frac{-145}{12}$$

or

Ans :

22. In the figure given below, ABCD is a rectangle. Find the values of x and y.

[Board Term-1 2012, Set-30]



From given figure we have

$$x + y = 22$$

and
$$x - y = 16$$

Adding (1) and (2), we have
$$2x = 38$$

$$x = 19$$

Substituting the value of x in equation (1), we get

$$19 + y = 22$$

$$y = 22 - 19 = 3$$

x = 19 and y = 3.

23. Find the roots of the following quadratic equation : $(x+3)(x-1) = 3(x-\frac{1}{3})$

Ans :

Hence,

We have

$$(x+3)(x-1) = 3\left(x-\frac{1}{3}\right)$$

$$x^{2}+3x-x-3 = 3x-1$$

$$x^{2}-x-2 = 0$$

$$x^{2}-2x+x-2 = 0$$

$$x(x-2)+1(x-2) = 0$$

$$(x-2)(x+1) = 0$$
Thus $x = 2, -1$

24. In a rectangle ABCD, E is a point on AB such that $AE = \frac{2}{3}AB$. If AB = 6 km and AD = 3 km, then find DE.

[Board Term-1 2016]

[Board Term-2 2012]

As per given condition we have drawn the figure below.



 $DE^2 = (3)^2 + (4)^2 = 25$

DE = 5 km

 $AE = \frac{2}{3}AB$ We have

$$B = \frac{2}{3} \times 6 = 4 \text{ km}$$

In right triangle ADE,

Thus



25. Show that :
$$\frac{\cos^2(45^\circ + \theta) + \cos^2(45^\circ - \theta)}{\tan(60^\circ + \theta)\tan(30^\circ - \theta)} = 1$$

Ans:

LHS =
$$\frac{\cos^2(45^\circ + \theta) + \cos^2(45^\circ - \theta)}{\tan(60^\circ + \theta)\tan(30^\circ - \theta)}$$
$$= \frac{\cos^2(45^\circ + \theta) + \sin^2(90^\circ - 45^\circ + \theta)}{\tan(60^\circ + \theta)\cot(90^\circ - 30^\circ + \theta)}$$
$$= \frac{\cos^2(45^\circ + \theta) + \sin^2(45^\circ + \theta)}{\tan(60^\circ + \theta)\cot(60^\circ + \theta)}$$
$$= \frac{1}{1} = 1 = \text{RHS}$$
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[Board 2020 OD Standard]

If $\cos(40^\circ + x) = \sin 30^\circ$, find the value of x. Ans: [Board Term-1 2015]

We have

$$\cos(40^{\circ} - x) = \sin 30^{\circ}$$

$$\cos(40^{\circ} + x) = \sin(90^{\circ} - 60^{\circ})$$

$$\cos(40^{\circ} + x) = \cos 60^{\circ}$$

$$40^{\circ} + x = 60^{\circ}$$

$$x = 60^{\circ} - 40^{\circ} = 20^{\circ}$$

Thus $x = 20^{\circ}$.

26. Find the unknown values in the following table :

Class Interval	Frequency	Cumulative Frequency
0-10	5	5
10-20	7	x_1
20-30	x_2	18
30-40	5	x_3
40-50	x_4	30

Ans :

[Board Term-1 2016]

We have

$$x_{1} = 5 + 7 = 12$$

$$x_{2} = 18 - x_{1} = 18 - 12 = 6$$

$$x_{3} = 18 + 5 = 23$$

$$x_{4} = 30 - x_{3} = 30 - 23 = 7$$

and

Ans :

Calculate the median from the following data :

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Marks	0-10	10-20	20-30	30-40	40-50
Number of Students	5	15	30	8	2

or

[Board Term-1 2012]

We prepare following cumulative frequency table to find median class.

Marks	No. of students	c.f.
0-10	5	5
10-20	15	20
20-30	30	50
30-40	8	58

40-50	2	60
	N = 60	

 $N = 60 ; \frac{N}{2} = 30$ We have

Cumulative frequency just greater than $\frac{N}{2}$ is 50 and the corresponding class is 20-30. Thus median class is 20-20. 回於充回

Now
$$l = 20, f = 30, F = 20, h = 10$$

Median, $M_d = l + \left(\frac{\frac{N}{2} - F}{f}\right) \times h$
 $= 20 + \left(\frac{30 - 20}{30}\right) \times 10$
 $= 20 + \frac{100}{30} = 20 + \frac{10}{3}$
 $= 20 + 3.33$
Thus $M_d = 22.22$

Thus Md = 23.33

27. If α and β are the zeroes of the polynomial $f(x) = x^2 - 4x - 5$ then find the value of $\alpha^2 + \beta^2$

Ans : [Board 2020 Delhi Basic]

 $p(x) = x^2 - 4x - 5$ We have

Comparing it by $ax^2 + bx + c$, we get a = 1, b = -4and c = -5

Since, given α and β are the zeroes of the polynomial,

Sum of zeroes,
$$\alpha + \beta = -\frac{b}{a} = \frac{-(-4)}{1} = 4$$

and product of zeroes, $\alpha\beta = \frac{c}{a} = \frac{-5}{1} = -5$

 $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$ Now,

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 $= (4)^2 - 2(-5)$

Find the quadratic polynomial, the sum and product of whose zeroes are -3 and 2 respectively. Hence find the zeroes.

Ans: [Board 2020 OD Basic]
Sum of zeroes
$$\alpha + \beta = -3$$
 ...(1)
and product of zeroes $\alpha\beta = 2$

Thus quadratic equation is

$$x^{2} - (\alpha + \beta)x + \alpha\beta = 0$$
$$x^{2} - (-3)x + 2 = 0$$
$$x^{2} + 3x + 2 = 0$$



Thus quadratic equation is $x^2 + 3x + 2 = 0$.

Now above equation can be written as

$$x^{2} + 2x + x + 2 = 0$$

$$x(x+2) + (x+2) = 0$$

$$(x+2)(x+1) = 0$$

one are -2 and -1.

28. Show that the sum of all terms of an AP whose first term is a, the second term is b and last term is c, is equal to $\frac{(a+c)(b+c-2a)}{2(b-a)}$

Ans :

Hence, zer

[Board 2020 OD Standard]

Given, first term, A = a $A_2 = b$ and second term D = b - aCommon difference, $A_n = c$ Last term, A + (n-1)d = ca + (n-1)(b-a) = c(b-a)(n-1) = c-a $n-1 = \frac{c-a}{b-a}$ $n = \frac{c-a}{b-a} + 1$ $=\frac{c-a+b-a}{b-a}$

 $n = \frac{b+c-2a}{b-a}$

Now sum of all terms

$$S_{n} = \frac{n}{2} [A + A_{n}] = \frac{(b + c - 2a)}{2(b - a)} [a + c]$$
$$= \frac{(a + c)(b + c - 2a)}{2(b - a)}$$
Hence Proved

or

If in an AP, the sum of first m terms is n and the sum of its first n terms is m, then prove that the sum of its first (m+n) terms is -(m+n).

Let 1^{st} term of series be a and common difference be d, then we have

and

$$\frac{m}{2}[2a + (m-1)d] = n \qquad \dots (1)$$

 $S_m = n$ $S_n = m$

$$\frac{n}{2}[2a + (n-1)d] = m \qquad \dots (2)$$

Subtracting we have

$$a(m-n) + \frac{d}{2}[m(m-1) - n(n-1)] = n - m$$

$$2a(m-n) + d[m^2 - n^2 - (m-n)] = 2(n-m)$$

$$2a(m-n) + d(m-n)[(m+n) - 1] = 2(n-m)$$

$$2a + d[(m+n) - 1] = -2$$

Now,

$$S_{m+n} = \frac{m+n}{2}[2a + (m+n-1)d]$$

$$= \frac{m+n}{2}(-2)$$
$$= -(m+n)$$

29. Two right triangles ABC and DBC are drawn on the same hypotenuse BC and on the same side of BC. If AC and BD intersect at P, prove that $AP \times PC = BP \times DP$.

Let ΔABC , and ΔDBC be right angled at A and D respectively.

As per given information in question we have drawn the figure given below.

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In $\triangle BAP$ and $\triangle CDP$ we have $\angle BAP = \angle CDP = 90^{\circ}$

and due to vertical opposite angle $\angle BPA = \angle CPD$ B١

y AA similarity we have

$$\triangle BAP \quad \sim \triangle CDP$$

Therefore
$$\frac{BP}{PC} = \frac{AP}{PD}$$

$$AP \times PC = BP \times PD$$
 Hence Proved

30. If $\sin\theta + \cos\theta = \sqrt{3}$, then prove that $\tan\theta + \cot\theta = 1$. [Board 2020 SQP Standard] Ans :

Given,
$$\sin \theta + \cos \theta = \sqrt{3}$$

Squaring above equation, we ha

$$\sin^2\theta + \cos^2\theta + 2\sin\theta\cos\theta = 3$$
$$1 + 2\sin\theta\cos\theta = 3$$

$$2\sin\theta\cos\theta = 3 - 1 = 2$$

$$\sin\theta\cos\theta\ = 1$$

Now,
$$\tan \theta + \cot \theta = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$$

$$= \frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}$$
$$= \frac{1}{\sin \theta \cos \theta}$$

Substituting value of $\sin\theta\cos\theta$ we have

$$\tan \theta + \cot \theta = \frac{1}{\sin \theta \cos \theta} = \frac{1}{1} = 1$$

31. Draw a line segment AB of length 8 cm. Taking A as centre, draw a circle of radius 4 cm, and taking B as centre draw another circle of radius 3 cm. Construct tangents to each circle of radius centre of the other circle.

[Board Term-2 Foreign 2017, OD 2014] Ans :

Steps of Construction :

- 1. Draw a line segment AB of length 8 cm.
- 2.Draw a circle with centre A and radius 4 cm.
- 3. Draw another circle with centre B and radius $3 \mathrm{~cm}$.
- 4. Taking AB as diameter draw another circle, which intersects first two circles at P and Q, and R and S.
- 5. Join B to P, B to Q, A to R and A to S. Thus BP, BQ, AR and AS are the required tangents.







32. In fig. *APB* and *AQP* are semi-circle, and AO = OB. If the perimeter of the figure is 47 cm, find the area of the shaded region. Use $\pi = \frac{22}{7}$.



Ans :

[Board Term-2 Delhi 2015]

We have redrawn the given figure as shown below;



Let r be the radius of given circle. It is given that perimeter of given figure is 47 cm.

$$2\pi r - \frac{1}{4}(2\pi r) + 2r = 47$$
$$\frac{3\pi r}{2} + 2r = 47$$
$$r\left(\frac{3}{2} \times \frac{22}{7} + 2\right) = 47$$
$$r\left(\frac{33}{7} + 2\right) = 47$$
$$r = \frac{47 \times 7}{47} = 7 \text{ cm}$$

Now, area of shaded region

$$A = \text{area of circle} -\frac{1}{4} \text{ area of circle}$$
$$= \frac{3}{4} \text{ area of circle}$$
$$= \frac{3}{4}\pi r^2 = \frac{3}{4} \times \frac{22}{7} \times 7 \times 7$$
$$= \frac{3}{2} \times 77 = 115.5 \text{ cm}^2$$

33. Find the mean of the following distribution by step deviation method :

Class	0-10	10- 20	20- 30	30- 40	40- 50	50- 60
Frequency	5	13	20	15	7	5

Ans :

[Board Term-1 2011]

Class	$egin{array}{c} x_i \ egin{array}{c} \mathbf{C} \ \mathbf{l} \ \mathbf{a} \ \mathbf{s} \ \mathbf{s} \ \mathbf{Marks} \end{pmatrix}$	$u_i = rac{x_i - a}{h}$	f_i	$f_i u_i$
0-10	5	-3	5	-15
10-20	15	-2	13	-26
20-30	25	-1	20	-20
30-40	35	0	15	0
40-50	45	1	7	7
50-60	55	2	5	10
	Total		$\sum f_i = 65$	$\sum f u_i = -44$

Let assumed mean, a = 35 and given h = 10.

Mean,

$$= 35 - 6.76 = 28.24$$

 $=35+\frac{-44}{65}\times 10$

 $M = a + \frac{\sum f_i u_i}{\sum f_i} \times h$

34. In figure O is the centre of a circle of radius 5 cm. T is a point such that OT = 13 cm and OT intersects circle at E. If AB is a tangent to the circle at E, find the length of AB, where TP and TQ are two tangents to the circle.



Ans: [Board Term-2 Delhi 2016]

Here $\triangle OPT$ is right angled triangle because PT is tangent on radius OP.

 $PT = \sqrt{13^2 - 5^2}$

Thus

and

 $= \sqrt{169 - 25} = 12 \text{ cm}$ TE = OT - OE

= 13 - 5 = 8 cm

Since length of tangents from an external point to a circle are equal,

Let PA = AE = x

Here $\triangle AET$ is right angled triangle because AB is tangent on radius OE.

In
$$\triangle AET$$
, $TA^2 = TE^2 + EA^2$
 $(TP - PA)^2 = 8^2 + x^2$
 $(12 - x)^2 = 64 + x^2$

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[Board Term-2 Foreign 2017]

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$$144 - 24x + x^2 = 64 + x^2$$
$$24x = 144 - 64 = 80$$

or,

Ans :

x = 3.3 cm.

Thus $AB = 2 \times x = 2 \times 3.3 = 6.6$ cm.

35. A solid toy is in the form of a hemisphere surmounted by a right circular cone. The height of the cone is 2 cm and the diameter of the base is 4 cm. Determine the volume of the toy. If a right circular cylinder circumscribes the toy, find the difference of the volume of the cylinder and toy. (Use $\pi = 3.14$)

[Board Term-2 2012]

Let BOC is a hemisphere and ABC is a cone. As per question the figure is shown below.



Radius of hemisphere is equal to the radius of cone which is $\frac{4}{2} = 2$ cm.

Height of cone, h = 2 cm

Volume of toy
$$= \frac{2}{3}\pi r^3 + \frac{1}{3}\pi r^2 h$$

 $\frac{1}{3}\pi r^2 (2r+h) = \frac{1}{3} \times 3.14 \times 2 \times 2(2 \times 2+2)$
 $= \frac{1}{3} \times 3.14 \times 4 \times 6$

$$= 25.12 \text{ cm}^3$$

Let right circular cylinder EFGH circumscribe the given solid toy.



Radius of cylinder = 2 cm

Height of cylinder = 4 cm

Volume of right circular cylinder

$$\pi r^2 h = 3.14 \times (2)^2 \times 4 \text{ cm}^3$$

= 50.24 cm³

Difference of two volume

$$= \text{Volume of cylinder} - \text{Volume of toy}$$
$$= 50.24 - 25.12 = 25.12 \text{ cm}^{3}.$$

- 36. A box contains 90 discs which are numbered 1 to 90. If one disc is drawn at random from the box, find the probability that it bears
 (i) a two digit number,
 - (ii) number divisible by 5.

Ans :

Total number of discs in the box are 90.

Thus we have 90 possible outcomes.

$$n(S) = 90$$

(i) a two digit number, Discs with two digit number are 10, 11,89 and 90 which are 81 numbers.

No. of favourable outcomes,

$$n(E_1) = 8$$

P(a disc with two digit number)

$$P(E_1) = \frac{n(E_1)}{n(S)} = \frac{81}{90} = \frac{9}{10}$$

(ii) number divisible by 5

The numbers divisible by 5 between 1 to 90 are 5, 10, 15 85 and 90 which are 18 numbers. No. of favourable outcomes,

 $n(E_2) = 18$

$$P$$
 (a disc with a number divisible by 5

$$P(E_2) = \frac{n(E_2)}{n(S)} = \frac{18}{90} = \frac{1}{5}$$

or

Two different dice are thrown together. Find the probability that the numbers obtained have

(i) even sum, and

(ii) even product.

Ans :

There are 36 possible outcomes of rolling two dices.

$$n(S) = 36$$

(i) even sum Favourable outcome are (1, 3), (1, 5), (1, 1), (2, 2), (2, 4), (2, 6), (3, 1), (3, 3), (3, 5), (4, 2), (4, 4), (4, 6)

(2, 4), (2, 6), (3, 1) (3, 3), (3, 5), (4, 2), (4, 4), (4, 6), (5, 1), (5, 3) (5, 5) (6, 2), (6, 4) and (6, 6). Number of favourable outcomes,

$$n(E_1) = 18$$

P(even sum),

$$P(E_1) = \frac{n(E_1)}{n(S)} = \frac{18}{36} = \frac{1}{2} \text{ or } 0.5$$

(ii) even product

Favourable outcome are (1, 2), (1, 4), (1, 6), (2, 1), (2,2), (2, 3), (2, 4), (2, 5), (2, 6), (3, 2), (3, 4), (3, 6), (4, 1), (4, 2), (4, 3), (4, 4), (4, 5), (4, 6), (5, 2), (5, 4), (5, 6), (6, 1), (6, 2), (6, 3), (6, 4), (6, 5) and (6, 6). Number of favourable outcomes

$$n(E_2) = 27$$

P(have a product less than 16),

$$n(E_2) = n(E_2) = 27 = 3$$

$$P(E_2) = \frac{n(E_2)}{n(S)} = \frac{21}{36} = \frac{3}{4} = 0.75$$

Probability of getting even product is $\frac{3}{4}$ or 0.75.

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